# Autonomous Evaluation of LLMs for Truth Maintenance and Reasoning Tasks

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### Motivation: Effective Human-Al Communication



Collaboration with AI requires clear, effective communication.

Promising approach: having the AI between the AI and the human.

- natural language (e.g., describing code)
- formal language (e.g., code, system specifications)



This approach is already being used in vibe coding.

- Generates code from a prompt
- Explains the generated code

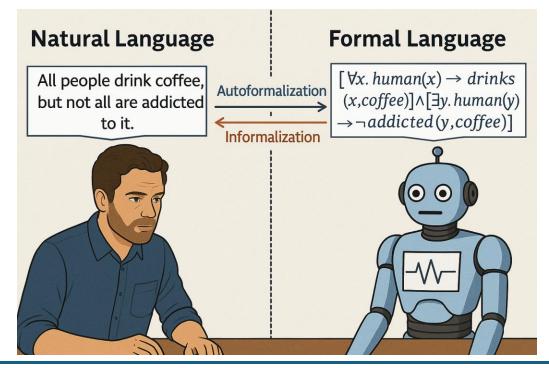
This requires the AI to be semantically accurate doing this translation.

# Objective: Assessment of LLM Truth Maintenance

Autoformalization: generating formal language from natural language.

Informalization: generating natural language from formal language.

Truth Maintenance: do these translations maintain semantic truth?

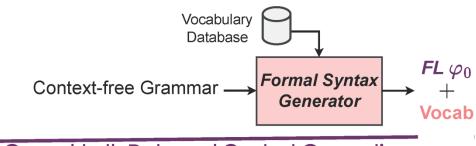


# Challenges With Current Approaches to LLM Assessment

- 1. Benchmark Contamination Problem: Risk of models training on evaluation data.
- 2. Difficult and expensive for expert annotators to construct new, high-quality datasets.
- 3. Incomplete set of ground truths (e.g., HumanEval) and imperfect existing autonomous evaluations metrics (e.g., BLEU) provide an inaccurate assessment of LLM capabilities.

BLEU("the weather is sunny and warm", "the weather is **not** sunny and warm") = 0.673

BLEU("the weather in Montreal is sunny and warm", "the weather in Montreal is **not** sunny and warm") = 0.767



Ground-truth Data and Context Generation

#### **Propositional Logic Context-Free Grammar**

$$S \to (S \land S)|(S \lor S)$$
  

$$S \to \neg S$$
  

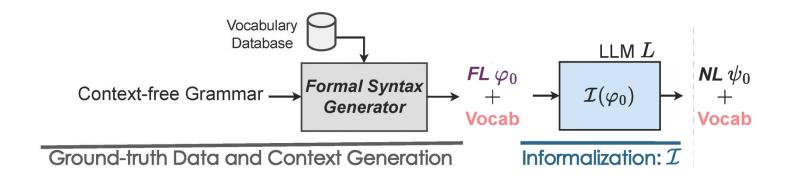
$$S \to \neg v|v$$

#### Formal Language String + Vocab

 $\varphi_0 = p_1 \wedge p_2 \wedge p_1$ 

 $p_1$ : it is raining

 $p_2$ : it was sunny yesterday



#### Formal Language String + Vocab

#### Informalization Using LLM $oldsymbol{L}$

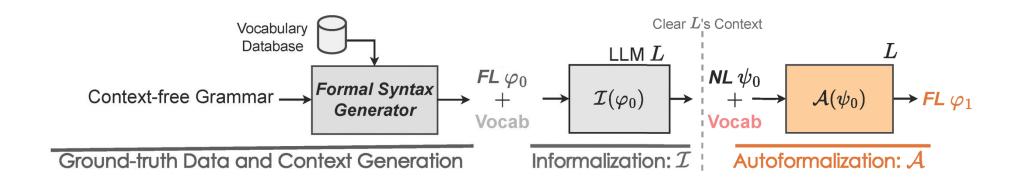
$$\varphi_0 = p_1 \wedge p_2 \wedge p_1$$

 $p_1$ : it is raining

 $p_2$ : it was sunny yesterday



 $b_0 = \frac{\text{The sun was bright the day before}}{\text{whilst it is raining heavily today.}}$ 



#### **Natural Language String + Vocab**

#### Autoformalization Using LLM $oldsymbol{L}$

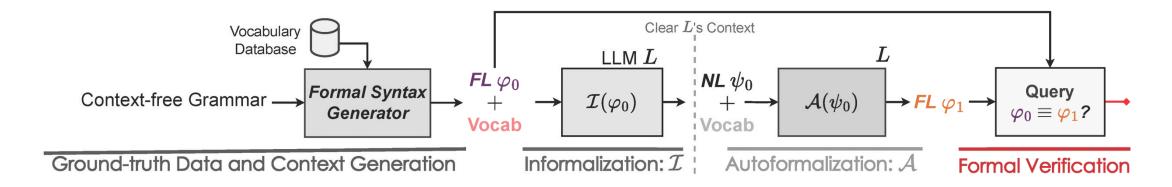
 $\psi_0 = { {
m The \ sun \ was \ bright \ the \ day \ before \ } \over {
m whilst \ it \ is \ raining \ heavily \ today.} }$ 

 $p_1$ : it is raining

 $p_2$ : it was sunny yesterday



$$\varphi_1 = p_1 \wedge p_2$$



# Original Formal Language String + Generated Formal Language String

#### **Formal Verification**

$$\varphi_0 = p_1 \wedge p_2 \wedge p_1$$

$$\varphi_1 = p_1 \wedge p_2$$



 $\varphi_0 \equiv \varphi_1$  (use semantic formal verifier (e.g., Prover9 for FOL))

- Done for propositional logic, first-order logic, and regular expressions.
- Can be extended to any formal language that has a semantic equivalence checker.

References: Prover9 [McCune, 2010].

## Theoretical Results

We prove the upper bound on false positive assessment rate.

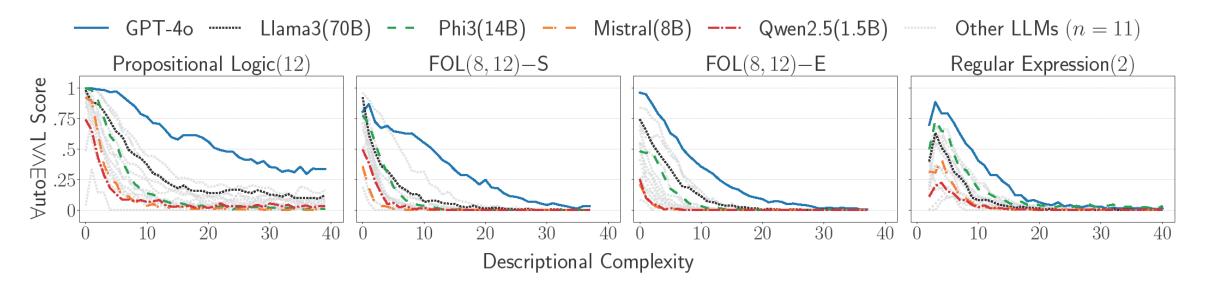
- $p_I$ : probability that an LLM L accurately informalizes formal language expression  $\varphi$ .
- $p_A$ : probability that L accurately autoformalize natural language expression  $\psi$ .
- $p_h$ : probability that if L hallucinates during both informalization and autoformalization that it will produce formal language equivalent to the original.

$$\varphi_0 \xrightarrow{I_L(\varphi_0)} \psi_0 \xrightarrow{A_L(\psi_0)} \varphi_1 \longrightarrow \cdots \xrightarrow{I_L(\varphi_{n-1})} \psi_{n-1} \xrightarrow{A_L(\psi_{n-1})} \varphi_n$$
$$\varphi_0 \equiv \varphi_1 \equiv \cdots \equiv \varphi_{n-1} \equiv \varphi_n$$

$$P(False\ Positive\ Assessment) = (1 - p_I)^n (1 - p_A)^n p_h^n$$

- 1. As LLMs improve,  $p_I \rightarrow 1$ ,  $p_A \rightarrow 1$ , and  $p_h \rightarrow 0$ .
  - Meaning,  $P(False\ Positive\ Assessment) \rightarrow 0$ .
- 2. Probability can be reduced by iteratively applying this process.

# Results: Truth Maintenance in Popular LLMs

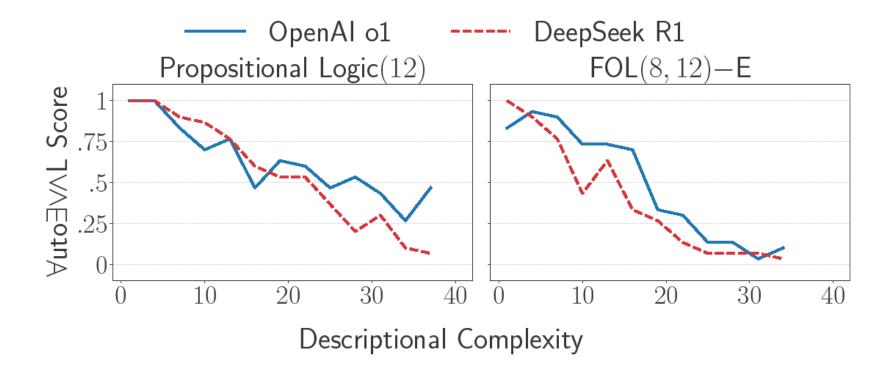


Evaluated 16 state-of-the-art, open and closed sourced LLMs.

- 3 types of formal language: propositional logic, first order logic, and regular expressions.
- 5 autogenerated datasets with approximately 85,000 unique evaluation examples.

All LLMs are less than 50% accurate on maintaining truth while translating formal language with 20 or more operators

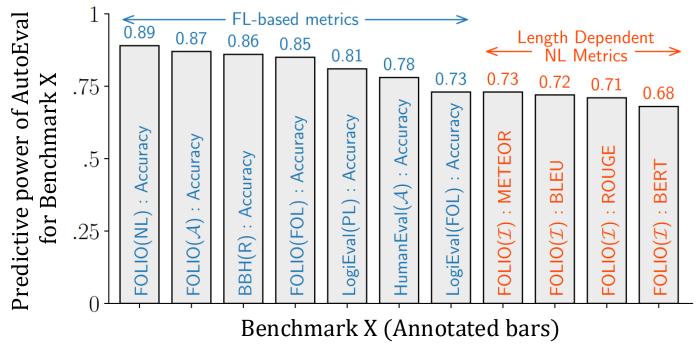
# Results: Truth Maintenance in Popular LRMs



State-of-the-art large reasoning models are at most 50% accurate on maintaining truth while translating logic with 25 or more operators.

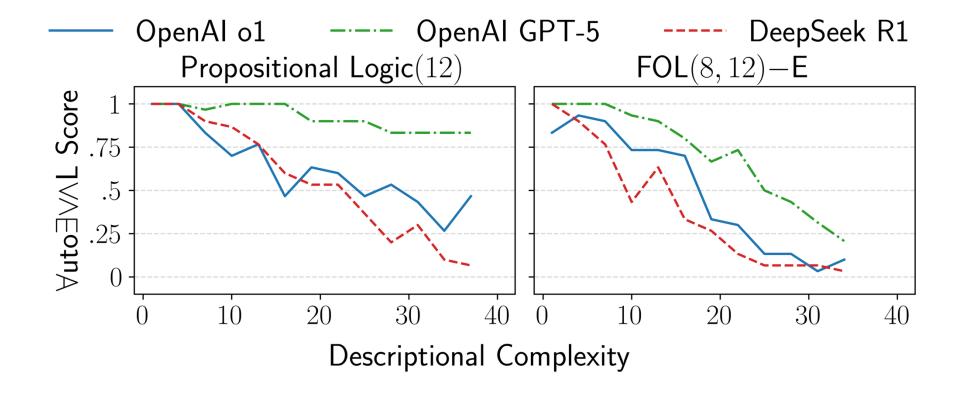
### Results: AutoEval Predicts Performance on Other Tasks

The predictive power of benchmark A for benchmark B: probability that an LLM that ranks better in A also ranks better in B  $[\Pr(L_1 \ge_B L_2 | L_1 \ge_A L_2)]$ .



A LLM's performance on AutoEval is predictive of its performance on reasoning tasks.

### New Results: GPT-5



Newer models are improving on this task, but there is still significant room for improvement

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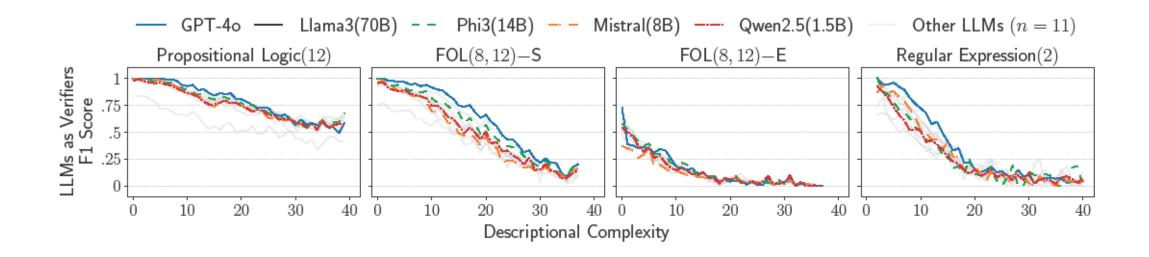




# Additional Results: LLMs as Equivalence Verifiers

Evaluated an LLM's to correctly evaluate whether the original and AutoEval process produced formal language were equivalent.

Measured the F1 score compared to the formal verifier.



All LLMs, regardless of size, perform similarly as equivalence verifiers.