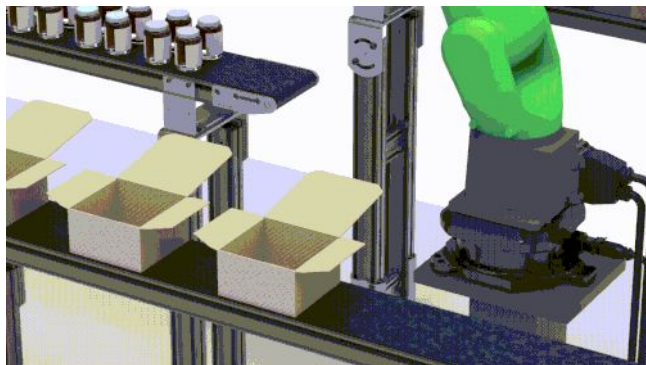


Inference of Human-derived Specifications of Object Placement via Demonstration

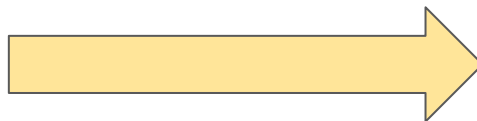
Alex Cuellar¹, Ho Chit Siu², Julie A Shah¹

¹ MIT, ² Lincoln Labs





Source: Linus Projects



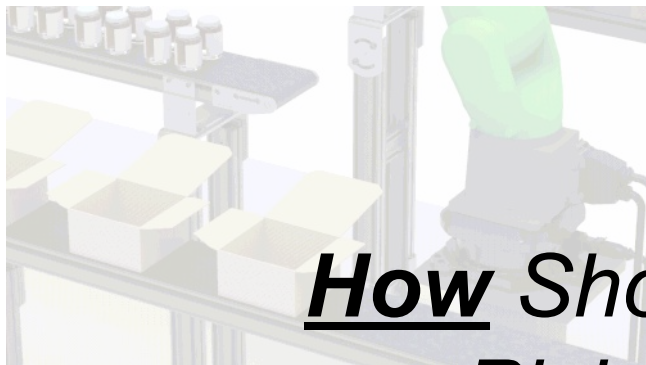
Dexterity
+
Perception



Source: Ambi Robotics



Source: Rutgers University



Source: Linus Projects

Question:

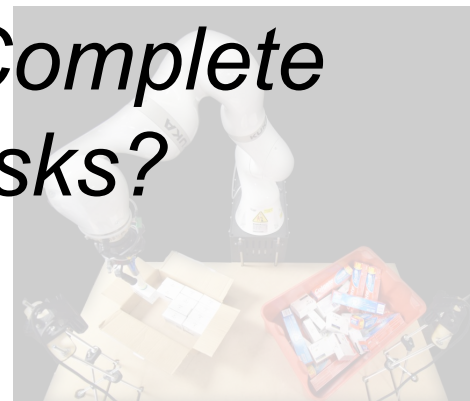


**How Should a Robot Complete
Pick-And-Place Tasks?**

Dexterity
Perception

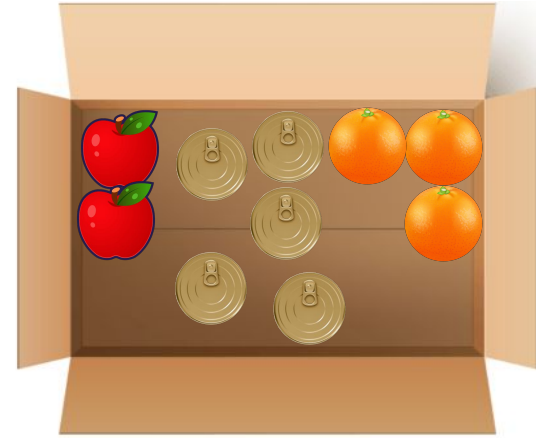
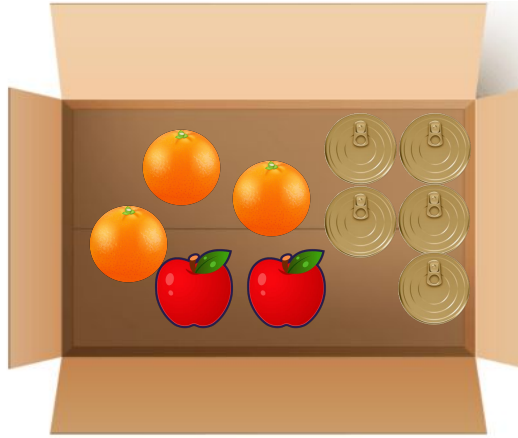
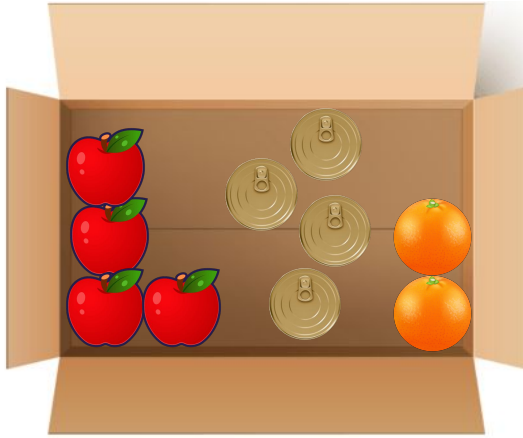


Source: Ambi Robotics

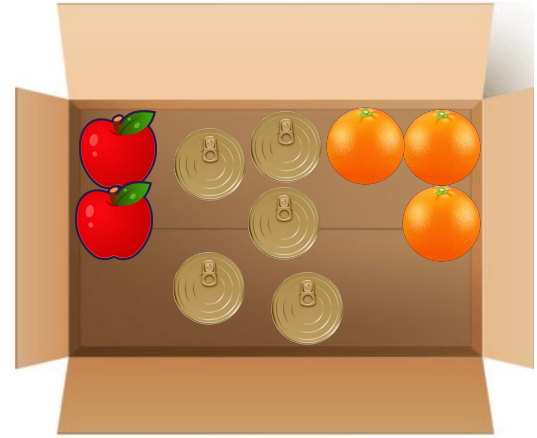
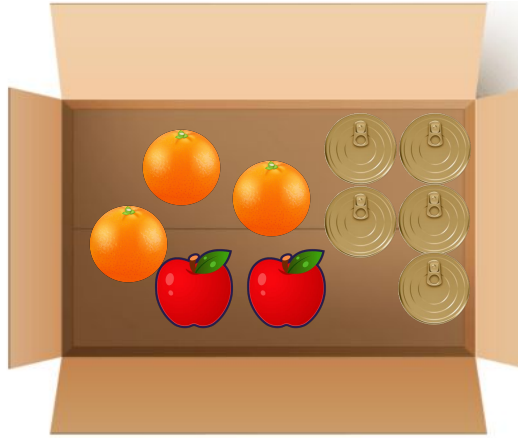
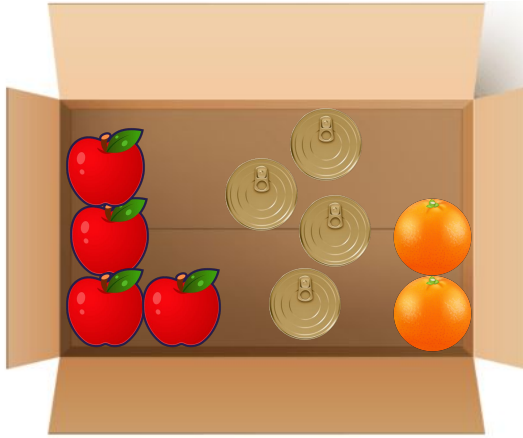


Source: Rutgers University

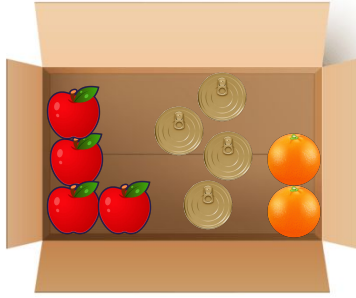
Which of These Doesn't Belong?



Which of These Doesn't Belong?



How do we know this?



Does not rely on:

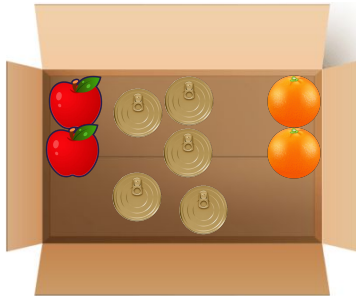
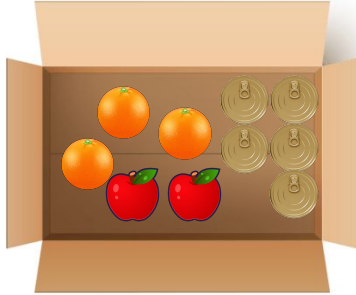
Exact Positions

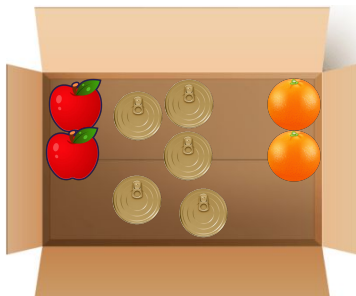
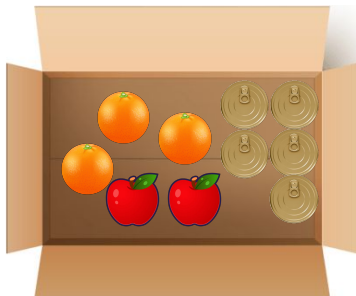
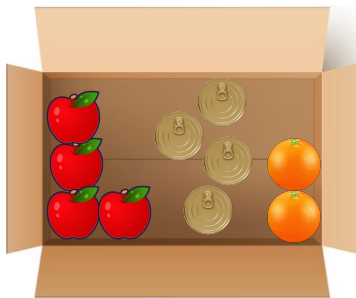
Individual Objects

Does rely on:

Spatial Relationships

Object “Types”





How do we know this?

Does not rely on:

Exact Positions

Individual Objects

Does rely on:

Spatial Relationships

Object “Types”

Why it Matters?

User Preference/ Expectation

“Apples are to the left of cans”

Requirements

“Fruit should be secured against box walls”

PARCC: Positionally Augmented Region Connection Calculus

A **specification language** defining requirements on the
spatial relationships between **classes of objects**

PARCC: Positionally Augmented Region Connection Calculus

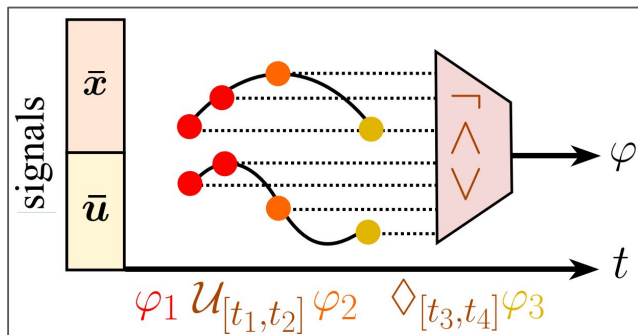
A **specification language** defining requirements on the **spatial relationships** between **classes of objects**

– AND –

An inference algorithm to **learn specifications**
from demonstrations

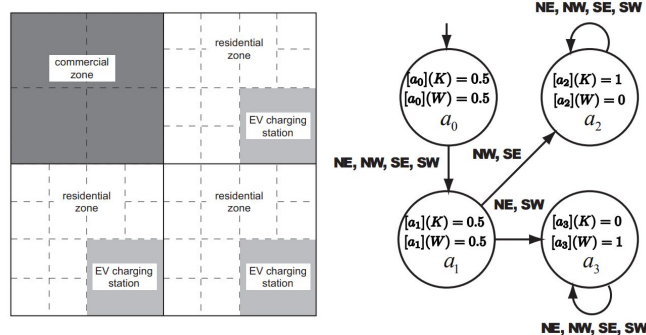
Existing Spatial Specification languages

Signal Temporal Logic [1]



Source: From [3]

Quad-Tree Representations [2]



Source: From Citation [3]

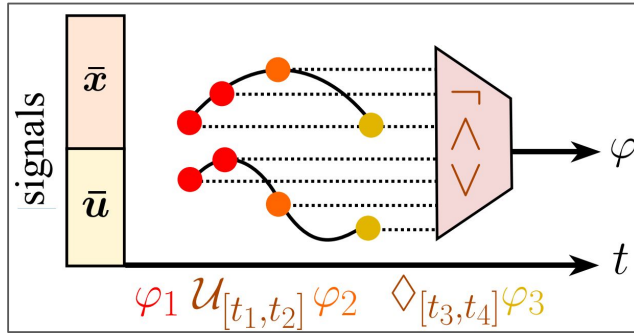
[1] Linard, Alexis, and Jana Tumova. "Active learning of signal temporal logic specifications." 2020 IEEE 16th International Conference on Automation Science and Engineering (CASE). IEEE, 2020.

[3] Haghighi, Iman, et al. "SpaTeL: a novel spatial-temporal logic and its applications to networked systems." Proceedings of the 18th International Conference on Hybrid Systems: Computation and Control. 2015.

[2] Gu, Zhaoyuan, et al. "Walking-by-logic: Signal temporal logic-guided model predictive control for bipedal locomotion resilient to external perturbations." IEEE International Conference on Robotics and Automation (ICRA). 2024.

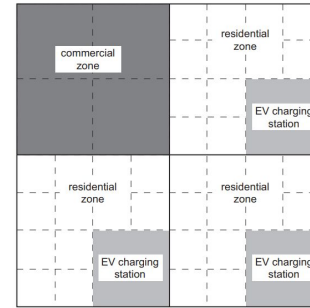
Existing Spatial Specification languages

Signal Temporal Logic [1]

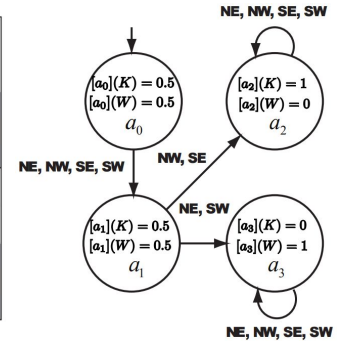


Source: From [3]

Quad-Tree Representations [2]



Source: From Citation [3]



Represent specifications over *specific regions* or *precise distance* in space

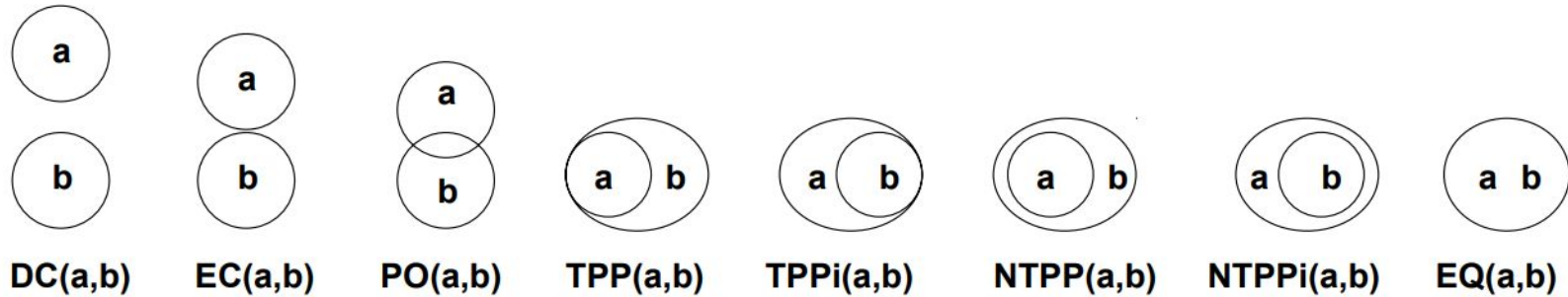
Don't easily represent *relationships between objects*

[1] Linard, Alexis, and Jana Tumova. "Active learning of signal temporal logic specifications." 2020 IEEE 16th International Conference on Automation Science and Engineering (CASE). IEEE, 2020.

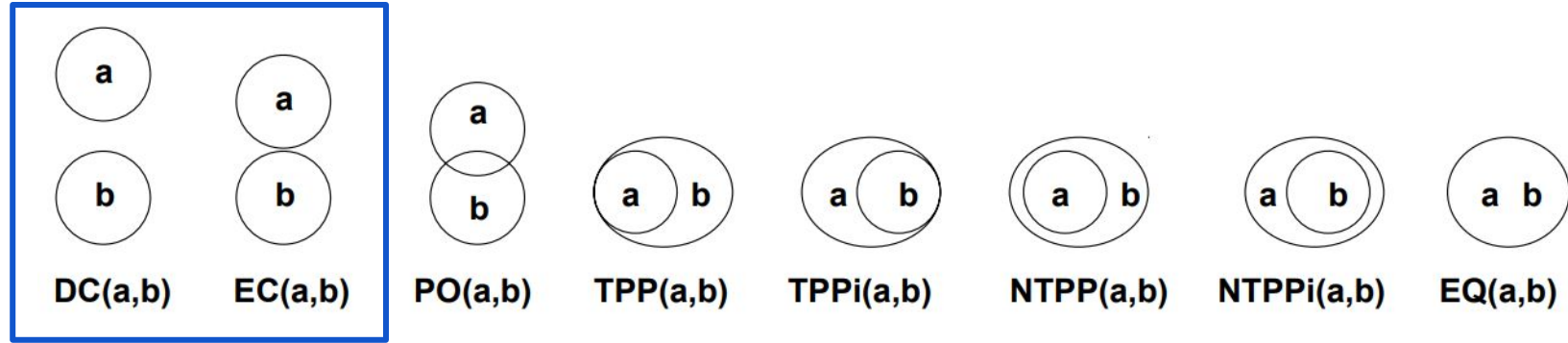
[3] Haghighi, Iman, et al. "SpaTeL: a novel spatial-temporal logic and its applications to networked systems." Proceedings of the 18th International Conference on Hybrid Systems: Computation and Control. 2015.

[2] Gu, Zhaoyuan, et al. "Walking-by-logic: Signal temporal logic-guided model predictive control for bipedal locomotion resilient to external perturbations." IEEE International Conference on Robotics and Automation (ICRA). 2024.

RCC: Reasoning Over Relationships of Spatial Regions

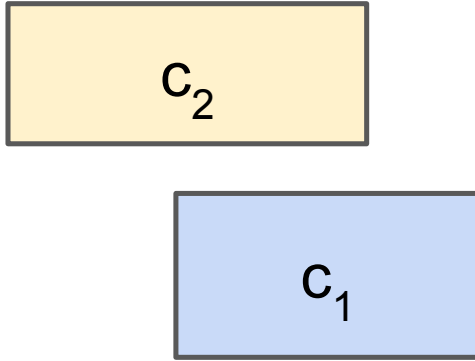


RCC: Reasoning Over Relationships of Spatial Regions



We use the fragment that assumes objects that do not share regions in space

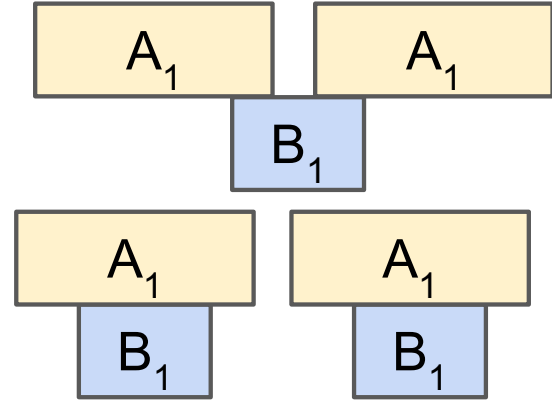
Defining PARCC: *Object Relations*



$$DR_N(c_2, c_1) \rightarrow DR(c_2, c_1) \wedge y_{c_2} \geq y_{c_1}$$
$$\forall (x_{c_2}, y_{c_2}) \in c_2, (x_{c_1}, y_{c_1}) \in c_1$$

PARCC “Object” Relationships

specify a direction (i.e. N,E,S,W)
between the objects it describes

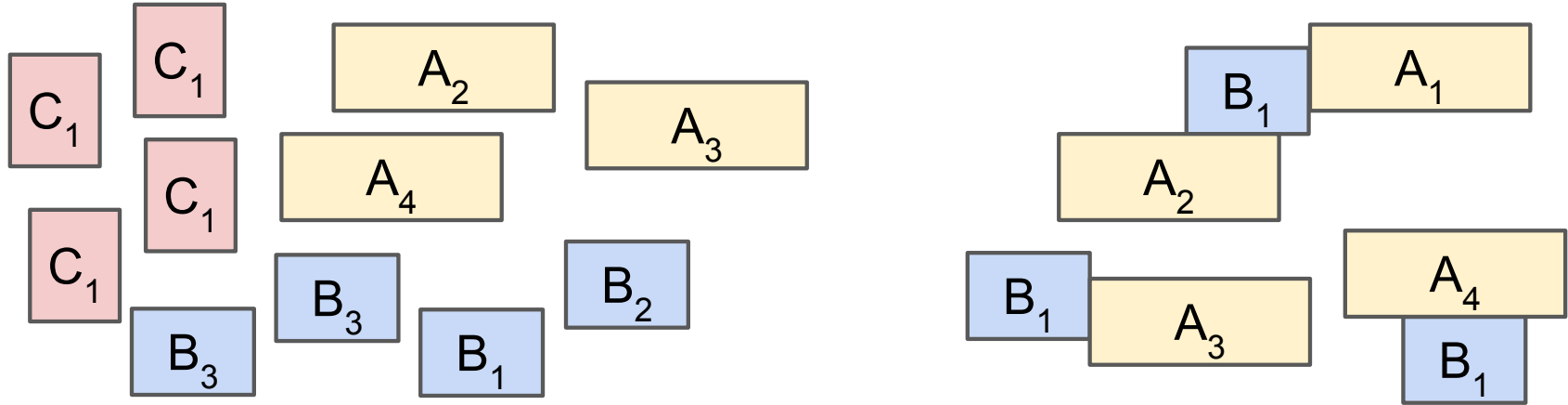


$$EC_N(A, B) \leftrightarrow EC_N(a, b)$$
$$\forall a \in \mathcal{A} \quad \exists b \in \mathcal{B}$$

PARCC “Class” Relationships:

Specify a relationship all objects of
one class have with another class

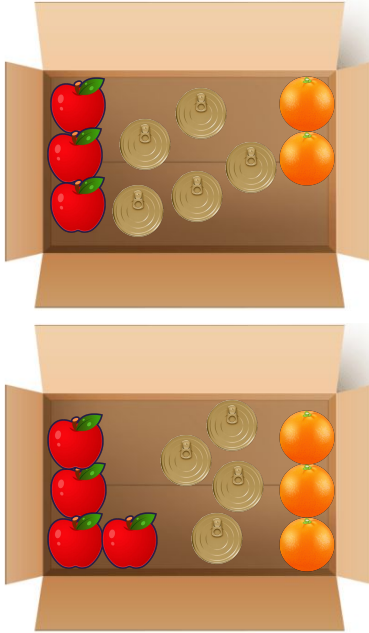
Defining PARCC: *Logical Specifications*



$$DR_N(A, B) \wedge DR_W(A, C) \quad EC_E(A, B) \vee EC_S(A, B)$$

PARCC Specifications utilize boolean logic to define requirements involving multiple class relations

Inferring PARCC Specifications

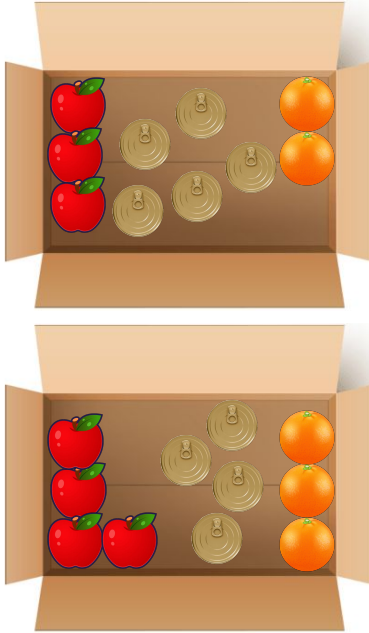


$$DR_E(O, C) \quad DR_W(A, C)$$

$$\bigvee_{i \in \{N, S, E, W\}} EC_i(O, O)$$

$$\bigvee_{i \in \{N, S, W\}} EC_i(A, W)$$

Inferring PARCC Specifications



Disjunctive “constraints”

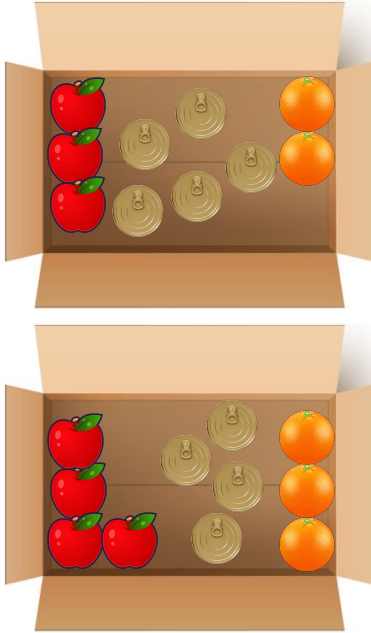
$$\mathcal{C} = \{\phi_1, \phi_2 \dots\}$$

$$DR_E(O, C) \quad DR_W(A, C)$$

$$\bigvee_{i \in \{N, S, E, W\}} EC_i(O, O)$$

$$\bigvee_{i \in \{N, S, W\}} EC_i(A, W)$$

Inferring PARCC Specifications



Disjunctive “constraints”

$$\mathcal{C} = \{\phi_1, \phi_2 \dots\}$$

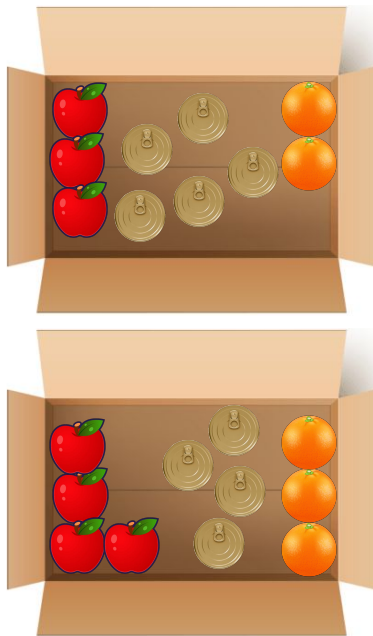
$$DR_E(O, C) \quad DR_W(A, C)$$

$$\bigvee_{i \in \{N, S, E, W\}} EC_i(O, O)$$

$$\bigvee_{i \in \{N, S, W\}} EC_i(A, W)$$

$$\text{Final Specification: } \Phi = \bigwedge_{\phi \in \mathcal{C}} \phi$$

Inferring PARCC Specifications



Disjunctive “constraints”

$$\mathcal{C} = \{\phi_1, \phi_2 \dots\}$$

$$DR_E(O, C) \quad DR_W(A, C)$$

$$\bigvee_{i \in \{N, S, E, W\}} EC_i(O, O)$$

$$\bigvee_{i \in \{N, S, W\}} EC_i(A, W)$$

$$\text{Final Specification: } \Phi = \bigwedge_{\phi \in \mathcal{C}} \phi$$

GOAL: Infer human's intended \mathcal{C}

Inferring PARCC Specifications

All Possible Disjunctive Formulas:

$N=1$:

$DR_W(A, C)$

$EC_E(O, A)$

$DR_N(A, O)$

...

$N=2$:

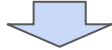
$DR_W(A, C) \vee DR_S(A, C)$

$EC_W(A, C) \vee DR_W(A, A)$

$EC_W(O, O) \vee DR_N(O, O)$

...

...



Satisfying Formulas:

$N=1$:

~~$DR_W(A, C)$~~

$EC_E(O, A)$

~~$DR_N(A, O)$~~

...

$N=2$:

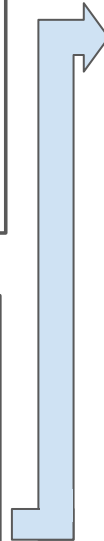
$DR_W(A, C) \vee DR_S(A, C)$

~~$EC_W(A, C) \vee DR_W(A, A)$~~

$EC_W(O, O) \vee DR_N(O, O)$

...

...



For each satisfying formula ϕ :

Probability that ϕ is incidentally satisfied:

$$P(D \rightarrow \phi | \mathcal{R}) =$$

$$\prod_{o \in \mathcal{O}_D^C} \max \left(\epsilon, \frac{\sum_{R \in \mathcal{R}} \sum_{o' \in \mathcal{O}_R^C} \mathbf{1}(o' \rightarrow \phi)}{\sum_{R \in \mathcal{R}} \sum_{o' \in \mathcal{O}_R^C} 1} \right)$$

$$P(D \rightarrow \phi | \mathcal{R}) < p_c :$$



Keep ϕ

$$P(D \rightarrow \phi | \mathcal{R}) > p_c :$$



Discard ϕ

Inferring PARCC Specifications

All Possible Disjunctive Formulas:

N=1:

N=2:

$DR_W(A, C)$ $DR_W(A, C) \vee DR_S(A, C)$...
 $EC_E(O, A)$ $EC_W(A, C) \vee DR_W(A, A)$...
 $DR_N(A, O)$ $EC_W(O, O) \vee DR_N(O, O)$...
 ...

Does this really capture human's ground truth object placement preferences?

N=1:

N=2:

~~$DR_W(A, C)$~~ $DR_W(A, C) \vee DR_S(A, C)$...
 $EC_E(O, A)$ ~~$EC_W(A, C) \vee DR_W(A, A)$~~ ...
 ~~$DR_N(A, O)$~~ $EC_W(O, O) \vee DR_N(O, O)$...
 ...

For each satisfying formula ϕ :

Probability that ϕ is incidentally satisfied:

$$P(D \rightarrow \phi | \mathcal{R}) =$$

$$\prod_{\phi \in \mathcal{C}_D} \max \left(\epsilon, \frac{\sum_{R \in \mathcal{R}} \sum_{o' \in \mathcal{O}_R^C} \mathbf{1}(o' \rightarrow \phi)}{\sum_{R \in \mathcal{R}} \sum_{o' \in \mathcal{O}_R^C} \mathbf{1}} \right)$$

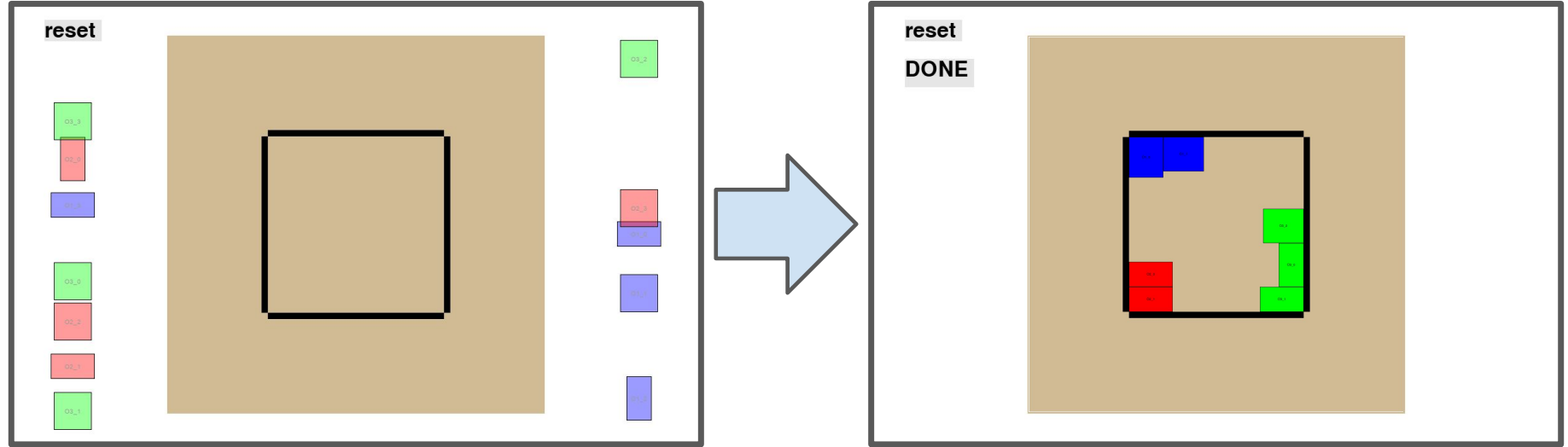
$$P(D \rightarrow \phi | \mathcal{R}) \leq p_c :$$

✓ Keep ϕ

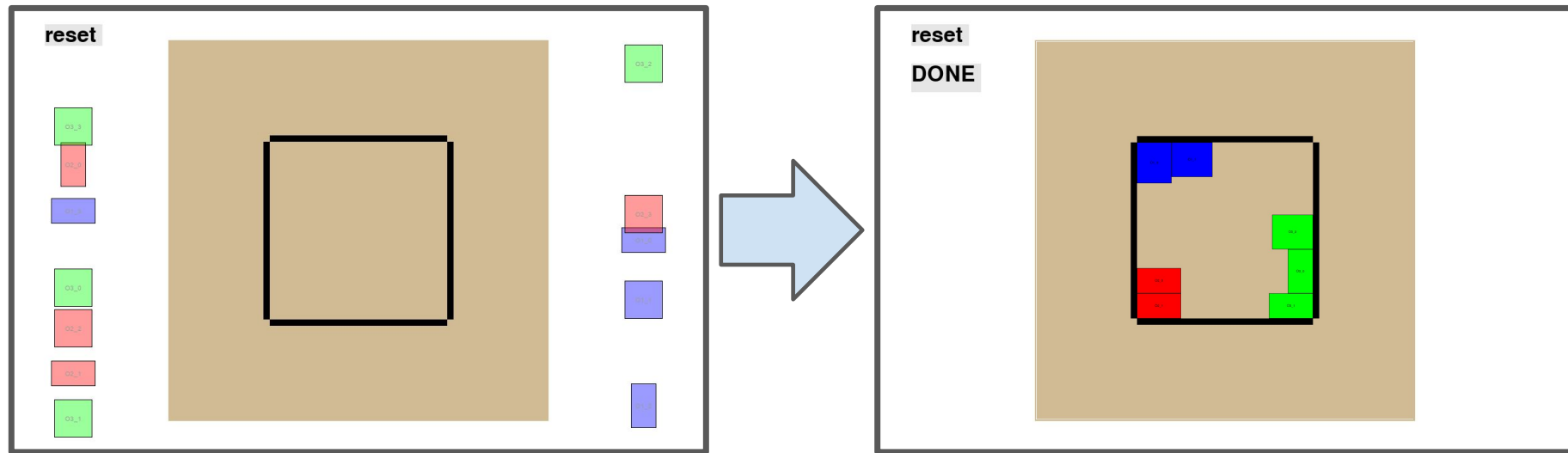
$$P(D \rightarrow \phi | \mathcal{R}) > p_c :$$

✗ Discard ϕ

Box Packing Domain



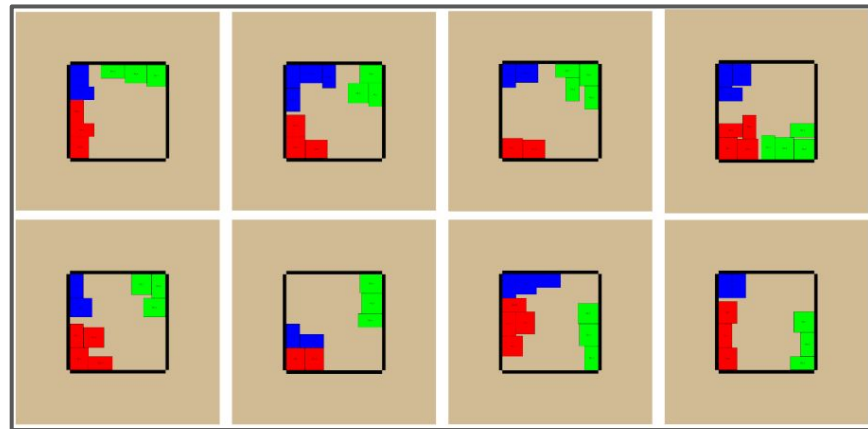
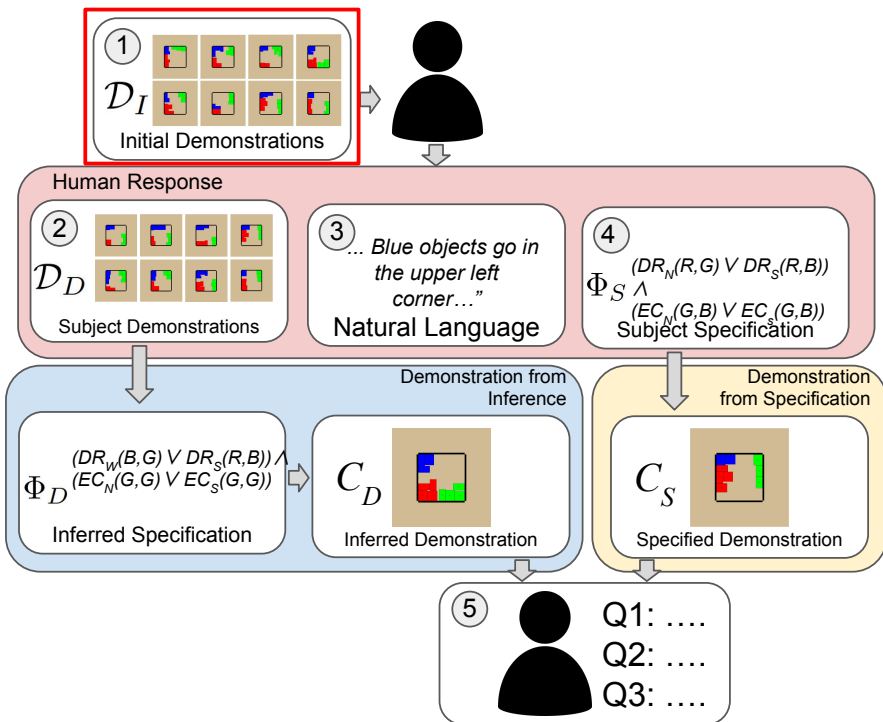
Box Packing Domain



Questions:

- Can the PARCC inference algorithm capture intuitive requirements on object placement?
- Can the inference algorithm capture requirements better than direct specification?

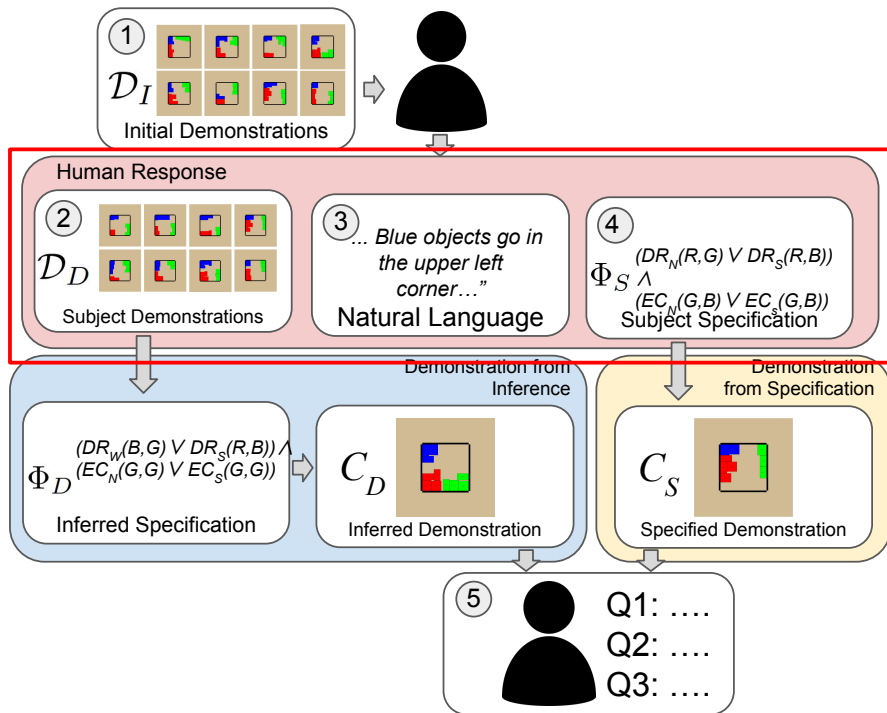
Human Study Design



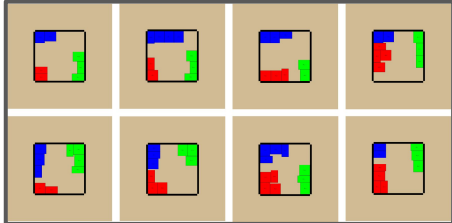
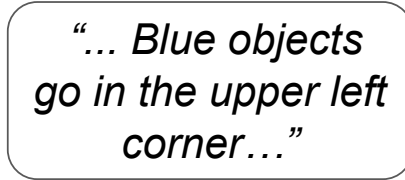
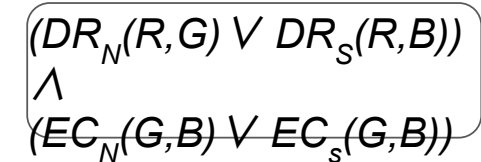
Show the participant 8 *initial demonstrations* that intentionally use a specification of 12 formulas:

$$\phi_1 \dots \phi_{12}$$

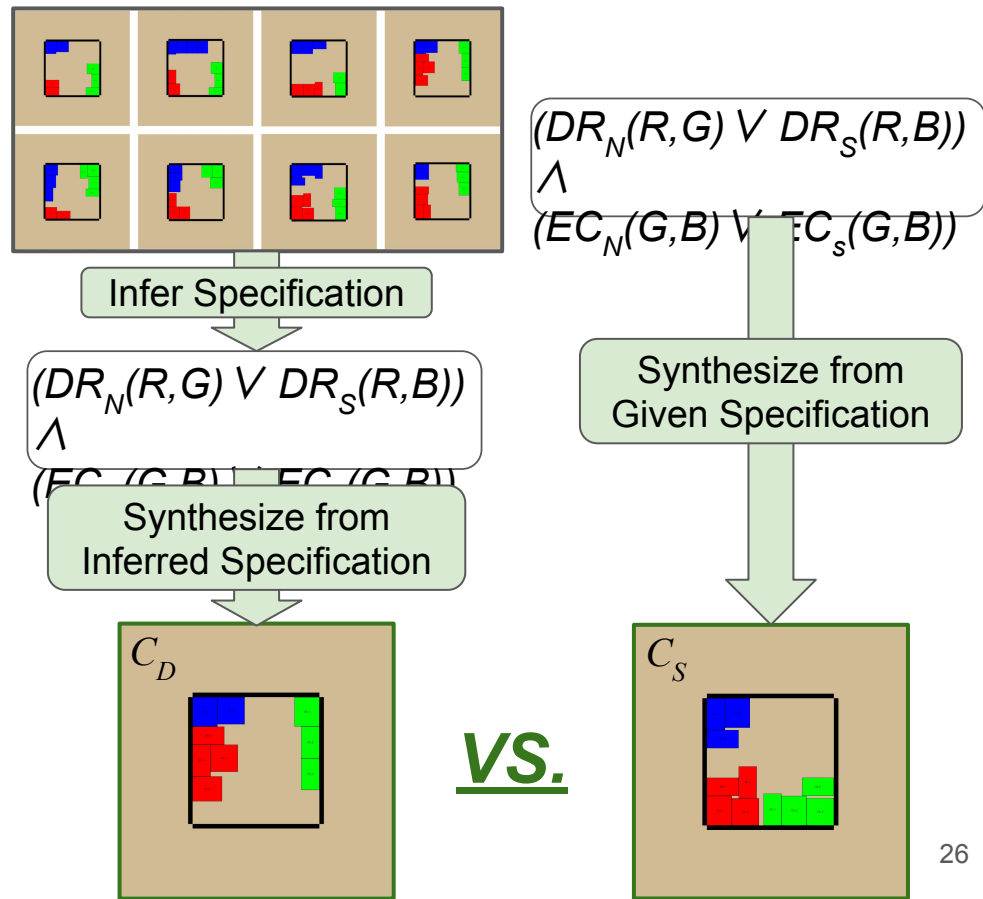
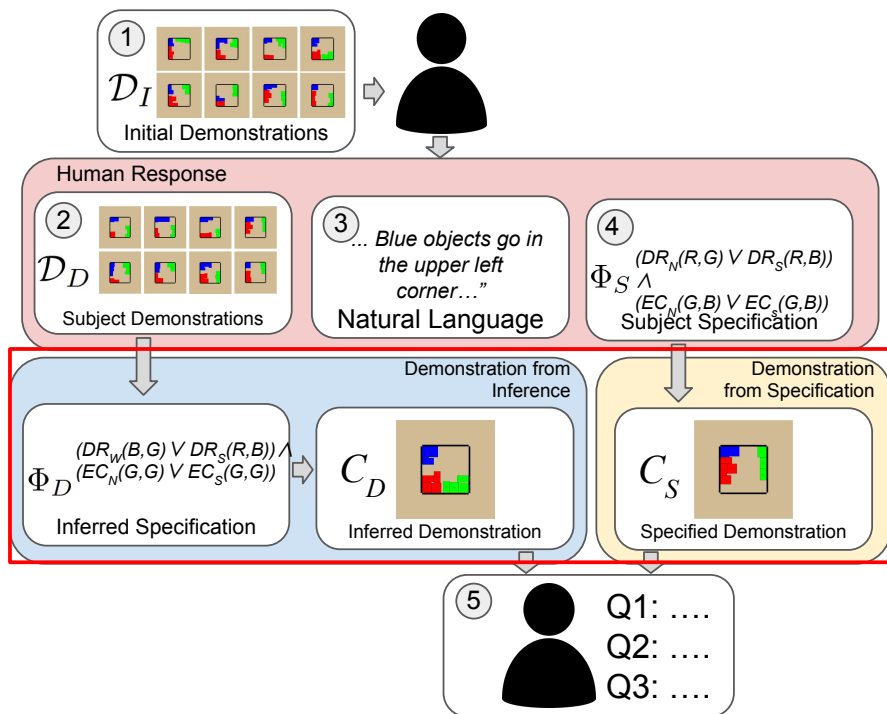
Human Study Design



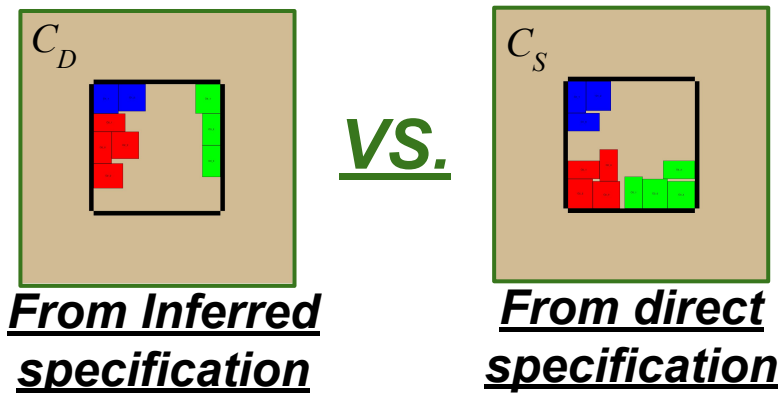
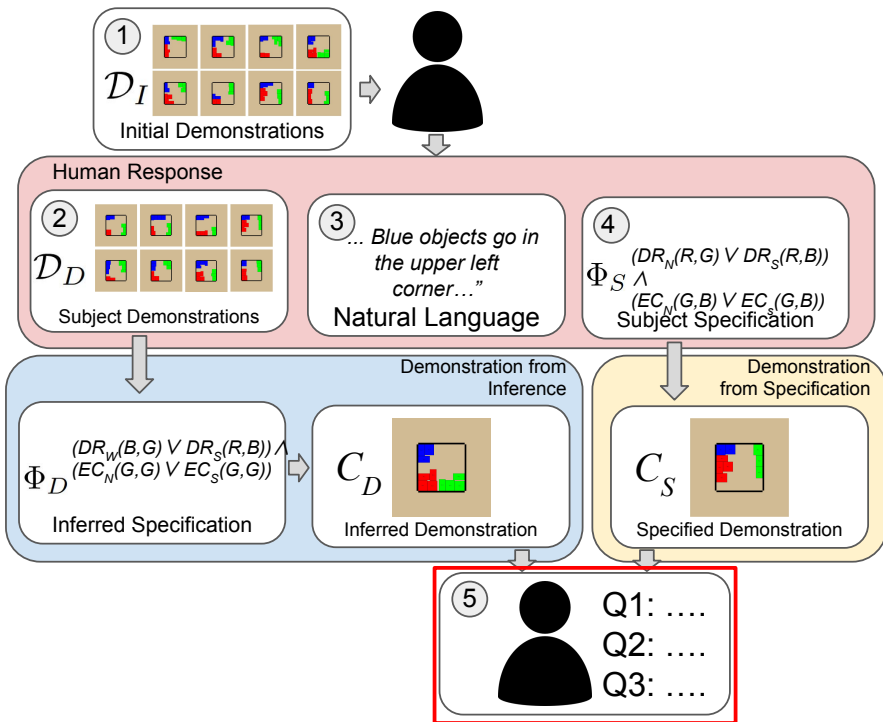
The subject provides:

- 1  Demonstrations matching the initial examples
- 2  Natural language description of requirements
- 3  PARCC specification

Human Study Design

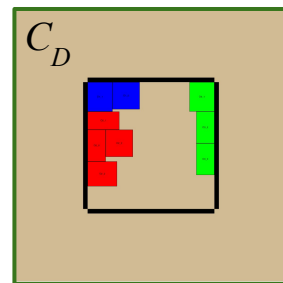
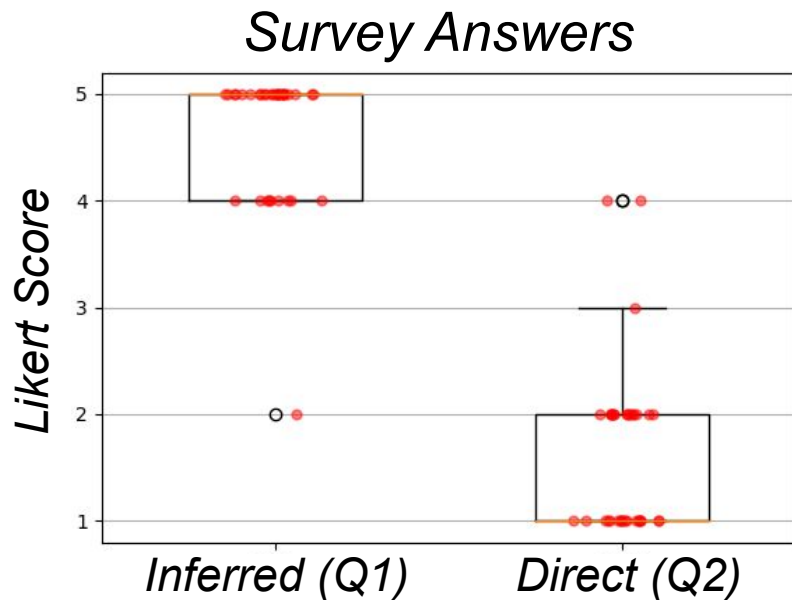


Human Study Design



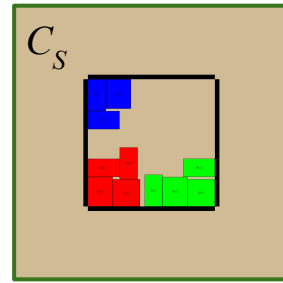
- 1) The *[inferred example]* matches patterns in my demonstrations.
- 2) The *[direct example]* matches patterns in my demonstrations.

Human Study Results: Inferred vs Direct Specifications



**From Inferred
specification**

VS.

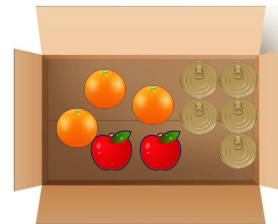
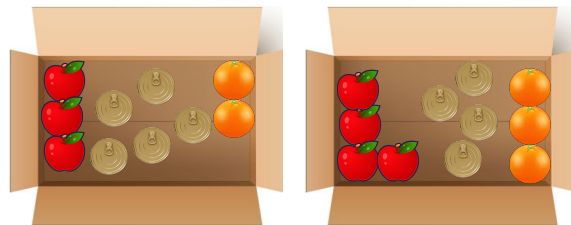


**From direct
specification**

- 1) The *[inferred example]* matches patterns in my demonstrations.
- 2) The *[direct example]* matches patterns in my demonstrations.

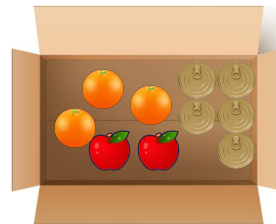
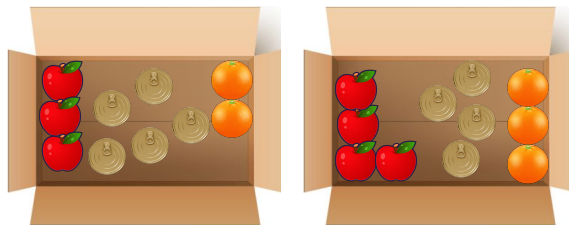
Limitations

- PARCC Representations:
 - Constrained to a 2D space
 - Only uses rectangular objects
- Inference Algorithm:
 - More efficient sampling of candidate disjunctions



Limitations

- PARCC Representations:
 - Constrained to a 2D space
 - Only uses rectangular objects
- Inference Algorithm:
 - More efficient sampling of candidate disjunctions



Questions?